

March 21

## GUIDED NOTES: Properties of Trapezoids and Kites

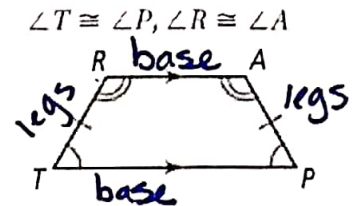
A **trapezoid** is a quadrilateral with exactly one pair of parallel sides, called *bases*, and two nonparallel sides, called *legs*.

### Isosceles Trapezoids

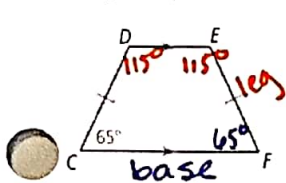
An **isosceles trapezoid** is a trapezoid with congruent legs.

A trapezoid is isosceles if there is only:

- One set of parallel sides (**bases**)
- Base angles are congruent
- Legs are congruent
- Diagonals are congruent
- Opposite angles are supplementary (**leg angles**)



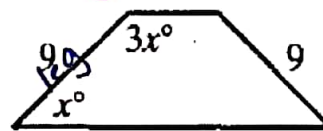
EX1: CDEP is an isosceles trapezoid and  $m\angle C = 65^\circ$ . What are  $m\angle D$ ,  $m\angle E$ , and  $m\angle F$ ?



$$\begin{aligned} \angle D &= 115^\circ \\ \angle E &= 115^\circ \\ \angle F &= 65^\circ \end{aligned}$$

$$180 - 65 = 115^\circ$$

EX2: The following is an isosceles trapezoid. What is the value of  $x$ ?

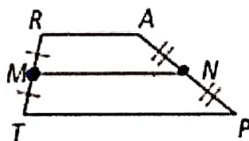


$$\begin{aligned} x + 3x &= 180 \\ 4x &= 180 \\ \frac{4x}{4} &= \frac{180}{4} \\ \boxed{x} &= \boxed{45} \end{aligned}$$

### Trapezoid Midsegment

The **median** (also called the midsegment) of a trapezoid is a segment that connects the midpoint of one leg to the midpoint of the other leg.

**Theorem:** If a quadrilateral is a trapezoid, then a) the midsegment is parallel to the bases and b) the length of the midsegment is half the sum of the lengths of the bases

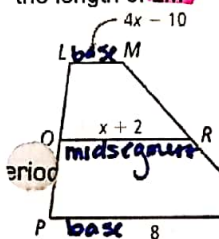


(1)  $\overline{MN} \parallel \overline{TP}$ ,  $\overline{MN} \parallel \overline{RA}$ , and

(2)  $MN = \frac{1}{2}(TP + RA)$

midsegment =  $.5(\text{base} + \text{other base})$

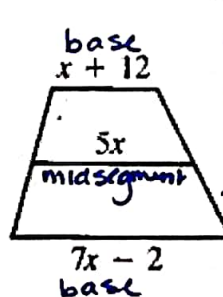
EX3: QR is the midsegment of trapezoid LMNP. What is  $x$  and the length of  $LM$ ?



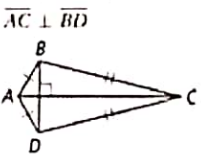
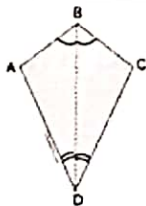
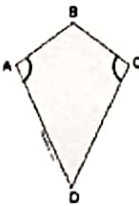
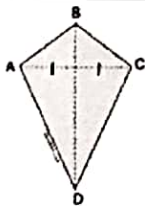
$$\begin{aligned} x + 2 &= .5(4x - 10 + 8) \\ x + 2 &= .5(4x - 2) \\ x + 2 &= 2x - 1 \\ -2x &= -3 \\ \frac{-2x}{-2} &= \frac{-3}{-2} \\ x &= \frac{3}{2} \end{aligned}$$

$$LM = 4\left(\frac{3}{2}\right) - 10 = \boxed{2}$$

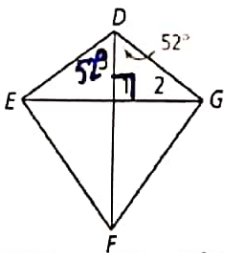
EX4: Find the length of the **midsegment**.



$$\begin{aligned} 5x &= .5(x + 12 + 7x - 2) \\ 5x &= .5(8x + 10) \\ 5x &= 4x + 5 \\ -4x &= -4x \\ x &= 5 \\ 5(5) &= \boxed{25} \end{aligned}$$

K i t e	A kite is a quadrilateral with two pairs of adjacent, congruent sides.	If a quadrilateral is a kite, then:			
		Its diagonals are perpendicular.	<del>Its</del> <sup>One</sup> diagonal bisects the opposite angles.	One pair of opposite angles are congruent.	One diagonal bisects the other.
		$\overline{AC} \perp \overline{BD}$ 			

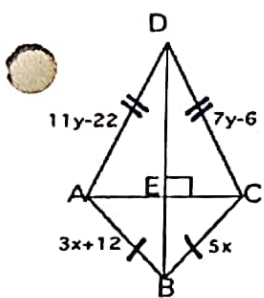
EX 5: Quadrilateral DEFG is a kite. What are  $m\angle 1$ ,  $m\angle 2$ , and  $m\angle 3$ ?



$$\begin{aligned} \angle 1 &= 90^\circ \\ \angle 2 &= 38^\circ \\ \angle 3 &= 52^\circ \end{aligned}$$

$$180 - 90 - 52 = 38^\circ$$

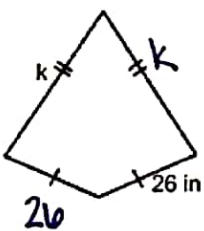
EX6: Quadrilateral ABCD is a kite. Solve for  $x$  and  $y$ .



$$\begin{aligned} 3x + 12 &= 5x \\ -3x & \quad -3x \\ \hline 12 &= 2x \\ \frac{12}{2} &= \frac{2x}{2} \\ 6 &= x \end{aligned}$$

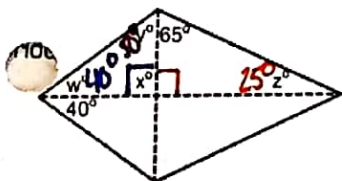
$$\begin{aligned} 11y - 22 &= 7y - 6 \\ -7y & \quad -7y \\ \hline 4y - 22 &= -6 \\ +22 & \quad +22 \\ \hline 4y &= 16 \\ \frac{4y}{4} &= \frac{16}{4} \\ y &= 4 \end{aligned}$$

EX7: Find  $k$  if the perimeter of the kite is 118 inches



$$\begin{aligned} k + k + 26 + 26 &= 118 \\ 2k + 52 &= 118 \\ -52 & \quad -52 \\ \hline 2k &= 66 \\ \frac{2k}{2} &= \frac{66}{2} \\ k &= 33 \end{aligned}$$

EX8: Find the missing information for the following kite.



$$180 - 90 - 65 = 25^\circ$$

$$180 - 90 - 40 = 50^\circ$$

$$\begin{aligned} w &= 40^\circ \\ x &= 90^\circ \\ y &= 50^\circ \\ z &= 25^\circ \end{aligned}$$