

March 5

Add/Subtract Rational Expressions With Common Denominators

Ex1 Simplify: $\frac{7x}{x+5} + \frac{(3x+1)}{x+5} = \frac{7x + (3x+1)}{x+5}$ * Keep the common denominators!

LCD: $x+5$

$$= \frac{7x + 3x + 1}{x+5}$$
$$= \frac{(10x+1)}{(x+5)}$$

* Factor and cancel if possible.

Ex2 Simplify: $\frac{(3m-4)}{5m^2} - \frac{(2m-3)}{5m^2} = \frac{(3m-4) - (2m-3)}{5m^2}$

LCD: $5m^2$

$$= \frac{3m - 4 - 2m + 3}{5m^2}$$
$$= \frac{(m-1)}{5m^2}$$

Ex3 Simplify: $\frac{x}{x^2+3x-10} + \frac{5}{x^2+3x-10} = \frac{x+5}{x^2+3x-10}$

LCD: $x^2+3x-10$

$$= \frac{(x+5)}{(x+5)(x-2)}$$
$$= \frac{1}{(x-2)}$$

$x^2+3x-10$
 $x^2 - 10 = -10x^2$
 $5x \quad -2x = 3x$

$$\begin{array}{r} x^2+5x-2x-10 \\ x \quad x \quad -2 \quad -2 \\ \hline x(x+5) - 2(x+5) \\ \hline (x+5)(x-2) \end{array}$$

Finding a Least Common Denominator

Ex4 Find the LCD for: $\frac{3}{(x-6)} + \frac{4}{x^2-8x+12}$

$x^2-8x+12$
 $x^2 \cdot 12 = 12x^2$
 \uparrow
 $-2x + -6x = -8x$

$x^2-2x \quad -6x+12$
 $x \quad x \quad -6 \quad -6$
 $x(x-2) \quad -6(x-2)$
 $(x-2)(x-6)$

LCD: $(x-6)(x-2)$

Ex5 Find the LCD for: $\frac{8x+4}{(x-4)} - \frac{2x+7}{(x+4)}$

LCD: $(x-4)(x+4)$

Ex6 Find the LCD for: $\frac{k-1}{(k+3)(k-3)} + \frac{k-7}{(k+3)(k+3)}$

LCD: $(k+3)(k-3)(k+3)$

Ex7 Find the LCD for: $\frac{17}{10x^3y^6} - \frac{1}{6x^4y^4}$

10: 10, 20, 30, 40,
 6: 6, 12, 18, 24, 30

LCD: $30x^4y^6$

*use biggest exponent in LCD!